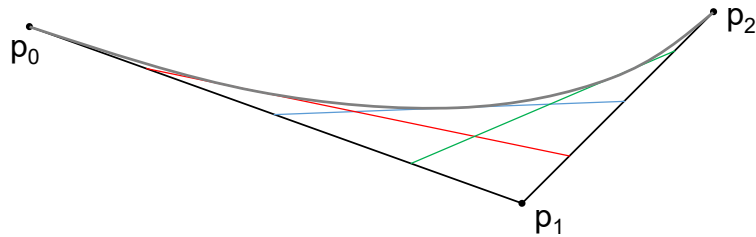


1. **2nd order (quadratic) Bézier curve:** Draw the Bézier curve with control points p_0, p_1, p_2 , using guiding points with $t = 0.25, 0.5, 0.75$.



2. Here is the parametric equation of a quadratic Bézier curve

$$Q(t) = (1-t)^2 p_0 + 2(1-t)t p_1 + t^2 p_2$$

- (a) Rearrange this function to make it look more like a quadratic in t (i.e. $Q(t) = at^2 + bt + c$).

$$Q(t) = p_0 - 2t p_0 + t^2 p_0 + 2t p_1 - 2t^2 p_1 + t^2 p_2$$

$$Q(t) = t^2 p_0 - 2t^2 p_1 + t^2 p_2 - 2t p_0 + 2t p_1 + p_0$$

$$Q(t) = (p_0 - 2p_1 + p_2) t^2 + (2p_1 - 2p_0) t + p_0$$

- (b) Take the derivative of this rearranged function with respect to t .

$$\frac{dQ}{dt} = 2(p_0 - 2p_1 + p_2)t + 2(p_1 - p_0)$$

- (c) What is the derivative at $t = 0$? $t = 1$? What can we say about the tangents at p_0 and p_2 ?

At $t = 0$, $\frac{dQ}{dt} = 2(p_1 - p_0)$, in other words it points from p_0 towards p_1 .

At $t = 1$, $\frac{dQ}{dt} = 2(p_0 - 2p_1 + p_2) + 2(p_1 - p_0) = 2(p_2 - p_1)$, so it points from p_1 towards p_2 .

3. **3rd order (cubic) Bézier curve:** Draw the Bézier curve with control points p_0, p_1, p_2, p_3 , using guiding points with $t = 0.25, 0.5, 0.75$.

