CSC 240: Computer Graphics Midterm Examination: Spring 2021 Due: Thursday, April 1 at 11:59 pm (on Moodle)

- This is a take-home exam with unlimited time from when it is out to when it is due. I don't expect you to work on it the entire time; it should take you just a few hours.
- It is open-notes, so you may use any course materials. If you use any online resources that haven't been part of this class, please cite them explicitly.
- You may not communicate or consult about the exam with anyone in the class (or outside the class, including requesting help by posting questions on the internet).
- You can post privately on Piazza if you need clarification on any question. If there is a clarification I think should be made to the entire class, I'll make the post public.
- I will still have office hours as usual, but I might not say much about the exam!
- Turn in your exam electronically on Moodle. (You may scan handwritten work.)
- If you are unable to make progress on any part of the exam, tell me what you tried: describe your thought process. I may be able to grant partial credit.
- When your exam is complete, before submitting it, please copy, sign, and date the statement below:

"I certify that my work on this exam adheres to the Smith Honor Code and the instructions given above. I have explicitly cited any resources used beyond my own notes and the materials available from the course web page."

Signed:

Date:

Name:	
Line drawing	/18
Fill algorithms	/16
Transformation matrices	/20
Animation	/10
Clipping	/20
Bézier splines	/16
Total	/100

Line Drawing (18 points)

Below are close-up images of portions of a drawing canvas. For each image, decide whether it could have been generated by using each of the algorithms listed below to draw just a single line.



Algorithms: (I.) simple midpoint algorithm, (II.) iterative midpoint algorithm, (III.) Wu's antialiased line.

Fill Algorithms (16 points)

Your friend is excited to learn about fill algorithms, and proposes two new ones for your consideration.

Algorithm A is a recursive algorithm. Instead of using a fixed order for the recursive calls, it always makes eight calls in a clockwise order starting from the square it just came from. So for example, when a recursive call is made to the north, the next calls will first try south, then southwest, then west, etc. If a recursive call is made to the west, the next calls will try east, then southeast, etc. The very first recursive call is always made to the north.

Algorithm B is an iterative sweep algorithm. When called, it will fill the current row by sweeping left then right just as we do in ordinary sweep fill. Then it will loop from the leftmost extent to the rightmost just as in ordinary sweep fill, but instead of making recursive calls it will instead do an iterative vertical sweep, filling up and then down until it hits a boundary. After each vertical sweep, it makes a recursive call to the left and the right at the very top, and again at the very bottom (but not at any pixels in the middle).

Your friend wants to know what you think of these ideas. Please answer for each algorithm:

- a.) Will it produce the same end result as the fill algorithms we have studied?
- b.) If not, describe the case(s) where the outcome differs. What sort of shapes give a different result?
- c.) How many recursive calls would each algorithm make to fill a 100x100 square region?
- d.) Compare your answer above to the number of recursive calls made by the two algorithms we studied.

Transformation Matrices (20 points)

Give the 2D transformation matrix that would accomplish each transformation shown below. (Hint: you can compose them out of the basic transformation types we studied.) Use homogeneous coordinates. The grid squares shown are all 1x1, and the Y axis is normal (not inverted as in screen coordinates). The black axis lines cross at the origin.



Animation (10 points)

In words, describe how you could use transformation matrices in conjunction with the HTML5 canvas graphics we have studied, to create an animation of a ball rolling across the screen from left to right. Make sure you specify the initial setup, and what happens during the animation. You don't need to give numbers, but you should be as specific as possible about what types of transformations are used, the order they are applied, and any other relevant details.

Clipping (20 points)

The drawing canvas is 80 pixels tall by 120 pixels wide. A triangle ABC is to be drawn with its corners at A = (-18,95), B = (32,-30), and C = (132,70).

- a.) Assuming that the clipping order is (top, bottom, right, left), draw the polygon after each stage of the Sutherland Hodgman clipping algorithm.
- b.) Compute coordinates for all the corners of the polygon once it is clipped to fit the screen.

Bézier Splines (16 points)

Consider the spline with control points (in sequential order): (0,1), (4,1), (1,4), (1,0).

- a.) Compute the (x,y) coordinates of three points on the curve, at t = 0.2, t = 0.5, and t = 0.8.
- b.) Draw a sketch of this curve.
- c.) The curve section mentioned is parameterized from t = 0 to t = 1. Suppose we want to extrapolate. What are the coordinates of the point at t = -1? At t = 2?
- d.) You want to extend the spline by adding another section. The new section should connect smoothly to the first at (1,0) and be a mirror image of it. What are the control points (in sequential order) of the new section?