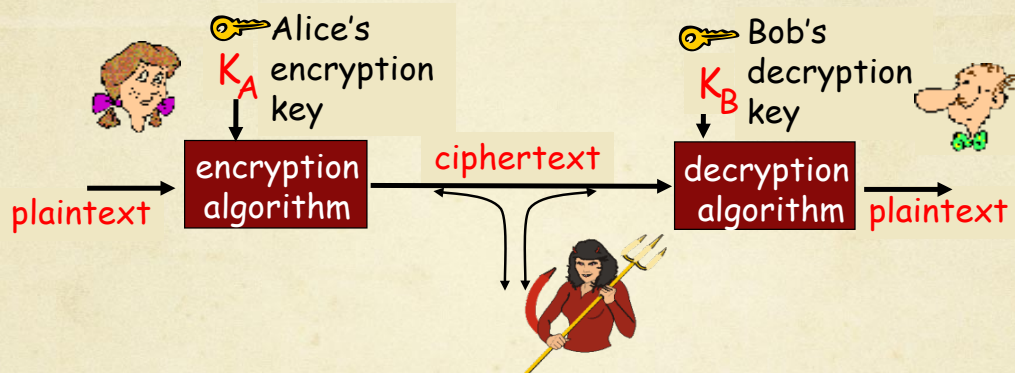




Network Security

- Symmetric Key Cryptography
 - Caesar cipher
 - DES and AES
- Public Key Cryptography

Cryptographic Keys



Symmetric key cryptography: sender & receiver keys are *identical* and *secret* (but known by 2 parties)

Public-key cryptography: the encryption key is *public*, the decryption key *secret*, and know only by one party

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Symmetric Key Cryptography

- Both parties have the same key
- Use this key to both encrypt and decrypt the message
 - The actions are symmetric
- **Early** - Caesar Cypher
- **Now**, two dominant algorithms
 - DES - data encryption standard
 - **AES** - advanced encryption standard

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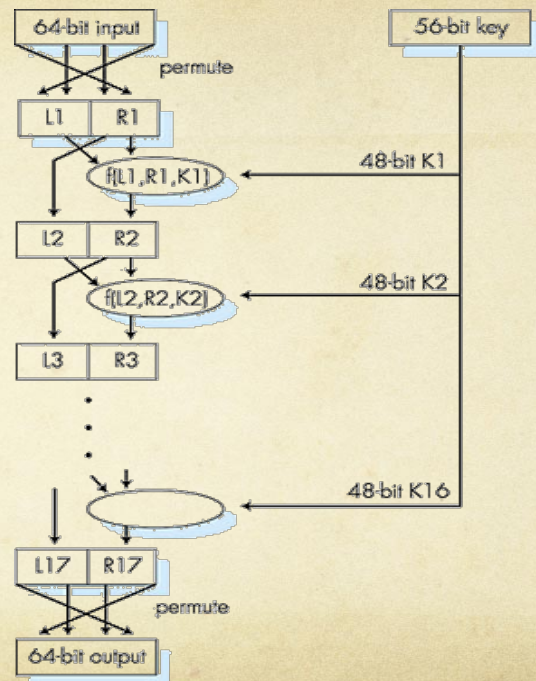
Symmetric key cryptography: DES

DES operation

Initial Permutation

16 identical “rounds” of function application, each using different 48 bits of key

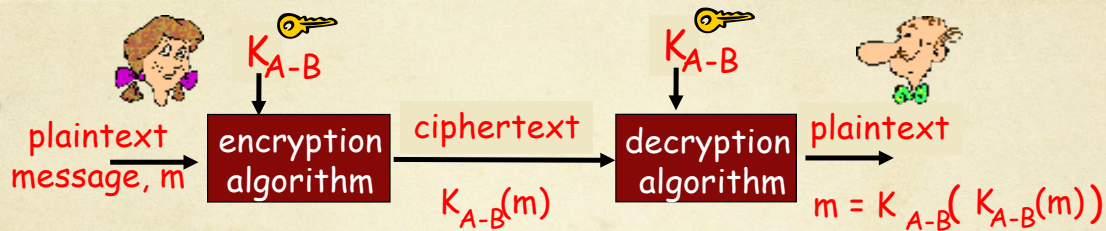
Final permutation



AES: Advanced Encryption Standard

- Symmetric-key NIST standard
 - Replaced DES (Nov 2001)
- Processes data in 128 bit blocks
 - 128, 192, or 256 bit keys
- Brute force decryption (try each key) taking 1 sec on DES, takes 149 trillion years for AES

Symmetric Key Cryptography

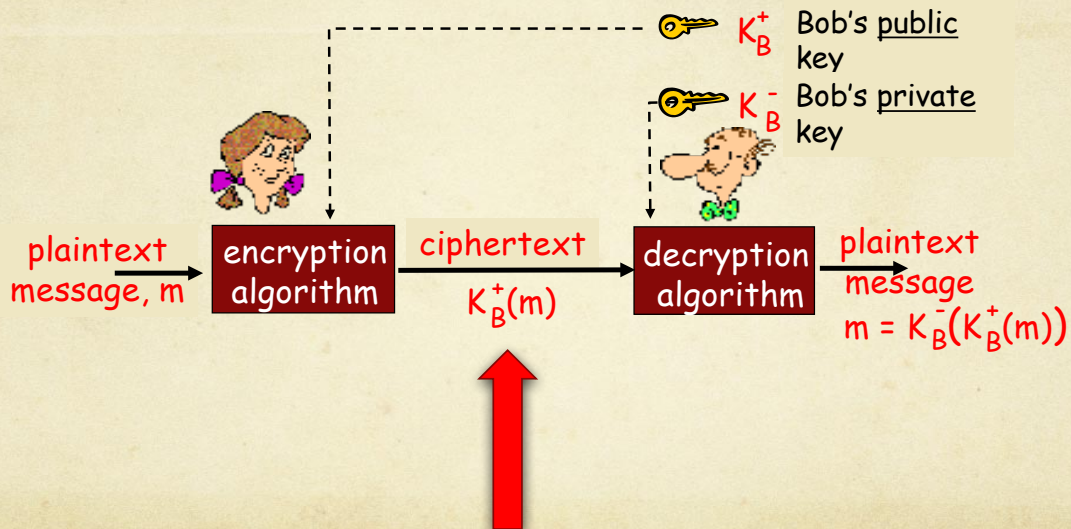


Symmetric key cryptography: Bob and Alice share/know the same (symmetric) key: K

- e.g., key is knowing substitution pattern in mono-alphabetic substitution cipher
- **Q:** how do Bob and Alice agree on key value?

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Public Key Cryptography



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RSA Important Property

The following property defines this method:

$$\underbrace{K_B^-(K_B^+(m))}_{\text{use public key first, followed by private key}} = m = \underbrace{K_B^+(K_B^-(m))}_{\text{use private key first, followed by public key}}$$

use public key
first, followed
by private key

use private key
first, followed
by public key

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Public key encryption algorithm

Requirements:

- 1 need $K_B^-(\bullet)$ and $K_B^+(\bullet)$ such that

$$K_B^-(K_B^+(m)) = m$$

- 2 given public key K_B^+ , it should be impossible to compute private key K_B^-

RSA: Rivest, Shamir, Adelson algorithm

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RSA: Choosing keys (an art)

1. Choose two large prime numbers p, q . (e.g., 1024 bits each)
2. Compute $n = pq$, $z = (p - 1)(q - 1)$
3. Choose e (with $e < n$) that has no common factors with z . (e, z are “relatively prime”).
4. Choose d such that $ed - 1$ is exactly divisible by z .
(in other words: $ed \bmod z = 1$).
5. Public key is (n, e) . Private key is (n, d) .
 K_B^+ K_B^-

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RSA: Encryption, Decryption

0. Given (n, e) and (n, d) as computed above
1. To encrypt bit pattern, m , compute
 $c = m^e \bmod n$ (i.e., remainder when m^e is divided by n)
2. To decrypt received bit pattern, c , compute
 $m = c^d \bmod n$ (i.e., remainder when c^d is divided by n)

Number
theory
result

$$m = \underbrace{(m^e \bmod n)}_c^d \bmod n$$

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RSA Example:

Bob chooses $p = 5, q = 7$. Then $n = 35, z = 24$.
 $e = 5$ (so e, z relatively prime).
 $d = 29$ (so $ed-1$ exactly divisible by z)

encrypt:	<u>letter</u>	<u>m</u>	<u>m^e</u>	<u>$c = m^e \bmod n$</u>
	I	12		
decrypt:	<u>c</u>	<u>c^d</u>	<u>$m = c^d \bmod n$</u>	<u>letter</u>

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* Activity *

- Using RSA, choose $p = 3, q = 11$. Encode a letter of your choice and send it to a different host to decode.
- Suggestion for e ? ... choose $e =$
- Then $z = (p-1)(q-1) =$
- Also choose $d =$
 -
 -
- Thus $n =$

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* Activity *

- So we have
 - $n = 33, e = 9, d = 9$
 - (n,d) & (n, e)
- Encrypt a **LETTER** and pass it across the room to be decrypted

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RSA in practice: session keys

- Exponentiation in RSA is computationally intensive
- DES/AES is at least 100 times faster than RSA
- Use public key crypto to establish secure connection, then establish second key – symmetric session key – for encrypting data

session key, K_S

- Bob and Alice use RSA to exchange a symmetric key K_S
- Once both have K_S , they use symmetric key cryptography

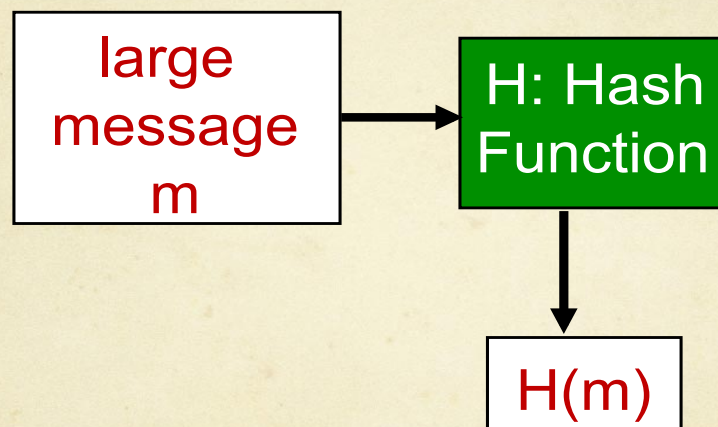
8-16

Next Security Tasks

- Encryption keys are public, so anyone could *claim* to be someone else
 - Need more than public key cryptography
- Ensure message is not corrupted
 - Message integrity with Message Authentication Code (MAC)
- Bind message to sender – end-point authentication
 - Digital signature
- ▣ Use: Cryptographic hash function

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Hash Functions



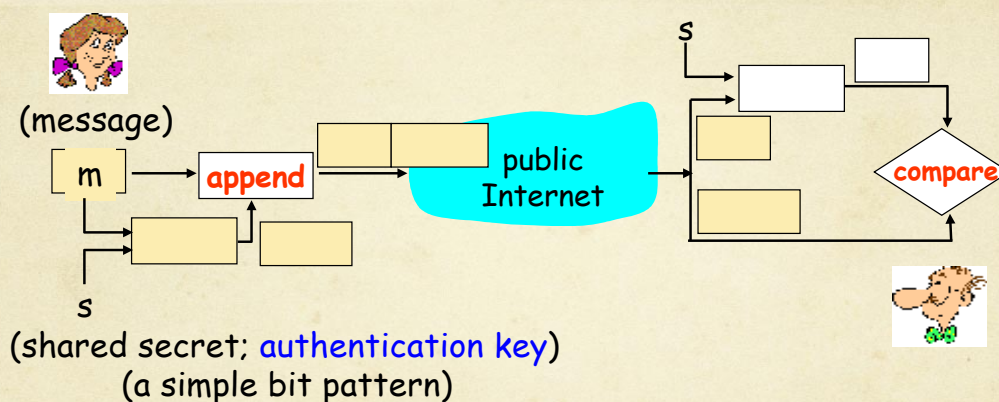
Cryptographic Hash Function

- The ideal cryptographic hash function has four properties:
 1. Easy to compute the hash value for any message, $H(m)$
 2. Infeasible to generate the message from the hash
 3. Infeasible to modify a message without changing the hash
 $H(m') \neq H(m)$
 4. Infeasible to find two different messages with the same hash
 $H(m1) \neq H(m2)$
- The **output** is called the *digest*
- **Note** – there is no encryption here

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(1) Message Authentication Code:

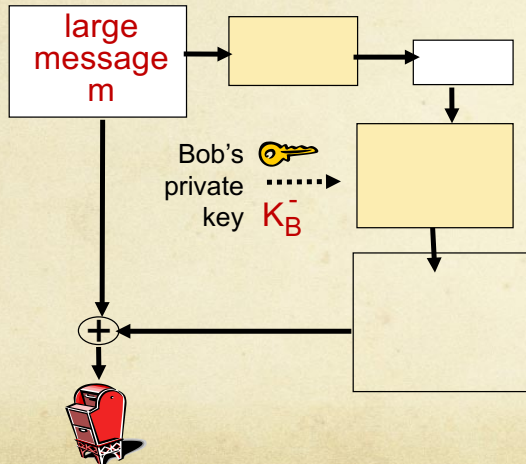
→ Use Shared Secret: $H(m+s) = \text{MAC}$



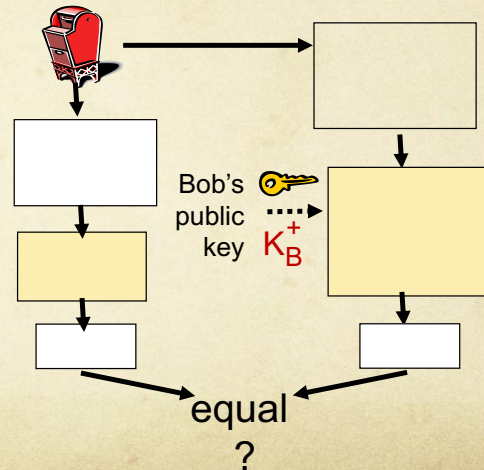
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Digital signature = signed message digest

Bob sends digitally signed message:



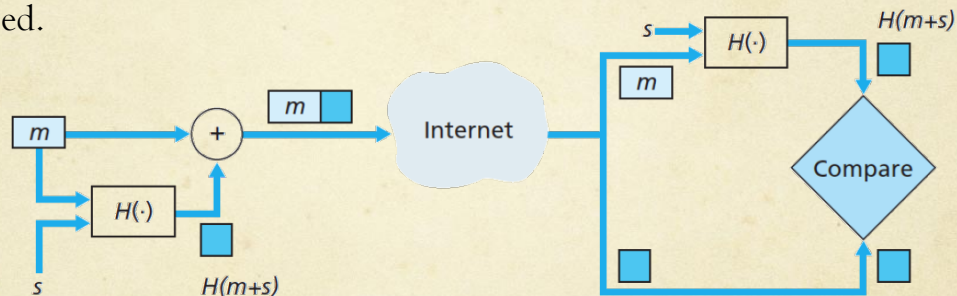
Alice verifies signature, integrity of digitally signed message:



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Task: Integrity + Authentication

- Suppose Alice and Bob share two secret keys:
 - an authentication key S_1 and
 - a symmetric encryption key S_2 .
- Augment the figure so that both integrity and confidentiality are provided.

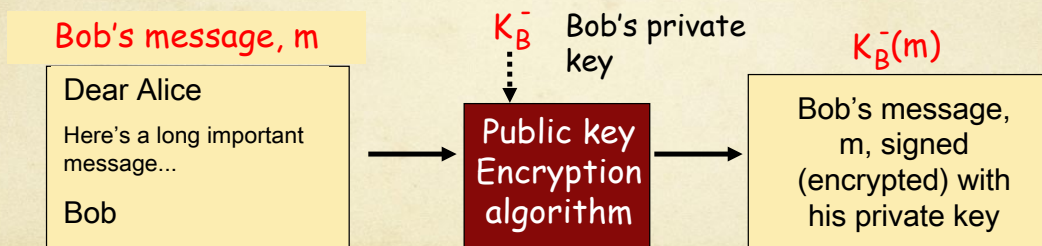


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(2) Digital Signature:

Use Public Key Cryptography

- Bob signs m by encrypting it with his private key K_B^- , creating “signed” message, $K_B^-(m)$
- Binds the message to the sender (stronger than $H(m+s)$)



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Digital Signatures (more)

- Alice verifies m signed by Bob by
 -
 -
- If $K_B^+(K_B^-(m)) = m$, whoever signed m must have used Bob's private key.

Alice thus verifies that:

- Bob signed m .
- No one else signed m .
- Bob signed m and not m' .

Non-repudiation:

- ✓ Alice can take m , and signature $K_B^-(m)$ to court and prove that Bob signed m .

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